

Acta Technica Napocensis: Civil Engineering & Architecture

Volume 60, No. 1, (2017)

Journal homepage: http://constructii.utcluj.ro/ActaCivilEng

ISSN 1221-5848



MECHANICAL AND SHRINKAGE BEHAVIOR OF FIBER REINFORCED SELF-COMPACTED CONCRETE

M. M. KAMAL, M. A. SAFANAND Z. A. ETMAN

Department of Civil Engineering - Faculty of Engineering- Menoufia University, Egypt

B. M. KASEM

Doctoral Fellow, Ministry of irrigation and public works

(Received 11 April 2017; Accepted 11 October 2017)

ABSTRACT

This research was conducted to evaluate the shrinkage behavior of fiber Self-Compacting Concrete (SCC) mixes. As the cement content in SCC mixes is usually high compared to normal concrete, the shrinkage is usually higher and the resistance against the development of induced cracks tends to be lower. The investigated mixes were fiber-reinforced utilizing steel and polypropylene fibers. The main parameters taken into consideration were the cement type, fiber type, volume fraction of fibers and different exposure conditions. Three types of fibers were used including hooked end steel fibers, cramped steel fibers and polypropylene fibers. The fresh properties of SCC were evaluated in terms of the slump, J-ring and V-funnel tests. The mechanical properties including the compression, splitting tensile as well as the modules of elasticity were measured. Also; the time-dependent deformations in terms of plastic and dry shrinkage were evaluated. Theoretical predictions of drying shrinkage were formulated. The results were compared to ACI and CEB equations of drying shrinkage..

Keywords: Self-compacting concrete, plastic shrinkage, dry shrinkage, Fibers, Mechanical Properties.

1. INTRODUCTION

Cement-based materials are the maximum considerable of all man-made materials substances and are among the most important construction materials. It is maximum probable that they will maintain to have the same importance in the future. However, such traditional construction and engineering materials are needed to meet new and better demands. Whilst dealing with troubles of productivity, economic system, great and surroundings, they must observe different production materials consisting of plastic, metal and wooden. One of the recent advances in concrete technology is the evolution of Self-compacted concrete (SCC). SCC is a brand new category of concrete that, without extra compaction power, flows and consolidates underneath the impact of its own weight [1]. Using SCC gives a basis for more industrialized production. not simplest will it lessen the bad tasks for workers, it could additionally reduce the technical costs of in situ concrete, due to the progressed casting cycle, quality, durability, surface finish, multiplied reliability of concrete structures and eliminating some of the potential human errors. However, SCC mixes are sensitive, strongly dependent on the composition and the characteristics of the constituents SCC mixes should possess the incompatible properties of high flowability together with high segregation resistance. This balance is made possible with the aid of the dispersing effect of high-range water reducing admixtures mixed with the cohesiveness produced by the high concentration of fine particles in additional filler material [2]. The principle mechanisms controlling this fine balance are related to surface physics and chemistry, hence, SCC is strongly dependent on the activity of the admixture, in addition to on the large surface area generated through the excessive content of fines [3]. Because the ratio of surface area to volume increases exponentially with particle irregularity and decreased size, this area has a principal impact on fresh and hardened concrete [4 - 7]. In almost all reinforced concrete structures, concrete is subjected to sustained stresses, and the load-dependent strains, as well as shrinkage strains, has profound

effects on the structural behavior. The consequences are the excessive deflection of the structural members, wide cracks in the concrete subjected to tensile stresses and redistribution of stresses with time. Moreover, the complexity of structures and their size have continued to increase, and this has led to a greater importance of their strain characteristics and deformation. The reinforced concrete designers possibly encounter far more problems. They need to know the creep and shrinkage properties of concrete and must be able to consider them in the analysis of concrete structures. Usually, shrinkage occurs simultaneously with creep, which is defined as deformation occurring under a constant sustained stress [8]. The common practice for decades has been to consider these phenomena to be additive. The overall increase in strain of a stressed and drying member is therefore assumed to consist of plastic shrinkage and creep. This technique is straight forward and appropriate for the many practical applications in which creep and shrinkage arise collectively. In fact, they are not independent and the principle of superposition cannot be applied [8, 9]. Previous studies have additionally tested the shrinkage of cement-limestone blends. While Bucher et al. [10] concluded that the fineness of the limestone influenced the shrinkage and stress, it should be noted that the systems evaluated consisted of cement with 10% additions of limestone of numerous sizes. As such, the cement-limestone blends have been no longer inter-ground and were not designed to have comparable overall performance like those typical of Portland Lime Stone Cements (PLCs). When inter-ground PLC mortar systems were evaluated, [11], and it was found that PLC systems were had similar or slightly less shrinkage than the Ordinary Portland Cement (OPC) systems. The PLC systems also had no increased tendency to crack. This study investigate the shrinkage of inter-ground PLCs containing up to 15% limestone and to better understand why these engineered PLCs do not appear to exhibit increased shrinkage with increased. The effect of different admixtures on shrinkage properties of self-compacted concrete was studied by Kar S. and Sanjay S. S [12]. They observed a positive effect for admixtures on the shrinkage of SCC. Ghezal, A. and Assaf, G. [13] studied the flexural creep behavior of self-compacted concrete by comparing its time-dependent behavior. In this study, the effect of adding randomly distributed short fibers to improve the shrinkage and toughness of cementitious matrices of SCC by preventing or controlling the initiation and propagation of cracks was studied. Twenty self compacting concrete mixtures were designed. Three types of fibers were used. Hooked end steel, cramped steel and polypropylene fibers were applied. Fly ash is used as mineral addition in order to achieve high powder content. Fresh properties of SCC were investigated (slump flow, viscosity and plastic shrinkage). In addition, the mechanical properties of the different mixes were tested (compressive strength, splitting tensile strength, flexural strength, elastic modulus and drying shrinkage).

2. EXPERIMENTAL PROGRAM

To achieve the aim of the research, twenty mixes were prepared from fiber reinforced self-compacted concrete (FSCC). Two types of cement (Portland cement and lime stone cement) were used. Two types of steel fibers (cramped and hooked end) were used with different volume fractions of 0.2, 0.75 and 1 %. Polypropylene fibers were used at 0.05, 0.1 and 0.2 % volume fraction. A total of 60 cylinders of 200 mm height and 100 mm diameter were tested in the fresh state to examine the plastic shrinkage of FSCC. A total of 120 cubes $100\times100\times100$ mm were tested to determine the compressive strength of the mixes at 7 and 28 days. A total of 180 cylinders of 300 mm height and 150 mm diameter were tested to determine the indirect tensile strength and modules of elasticity at 28 days. A total of 60 prisms $70\times70\times300$ mm were tested to determine the drying shrinkage of hardened concrete.

2.1 Materials

Two types of cement were used; ordinary Portland cement (CEM I 42.5 N) and Portland limestone cement (CEM II/B-L 32.5 N). Ordinary Portland cement conformed with the requirements of E.S.S. 4765-1/2009 [14] with a specific gravity of 3.16 and Blain fineness of 3994 cm²/gm. Portland limestone cement conformed with the requirements of E.S.S. 4765-1/2009 [14] with specific gravity of 3.15 and Blain fineness of 4850 cm²/gm. Crushed dolomite was used as a coarse aggregate with a maximum nominal size of 12 mm, a specific gravity of 2.75, absorption of 2.1% and a crushing modulus of 18.5%. Well graded siliceous sand was used with a specific gravity of 2.60, absorption of 0.81%, and a fineness modulus of 2.55. Class (F) fly ash meeting the requirements of ASTM C618 [15] with a specific gravity of 2.1 was used. The cement content was 400 kg/m³ in all mixes and the water per binder (fly ash+ cement) ratio (w/b) was 0.4. Tap water was used for mixing the concrete. A high range water reducer (HRWR) was used as superplasticizer meeting the requirements of ASTM C494 (Type A and F) [16]. The admixture is a brown liquid having a density of 1.18 kg/liter at room temperature. The amount of HRWR was 1.5% of the binder

(fly ash + cement) weight. The steel fibers used were either hooked end or cramped with a length of 25 mm, 1 mm in diameter and 7.85 g/cm^3 density. The polypropylene fibers were fibrillated with 15 mm length and 0.9 g/cm^3 density.

2.2 Casting and testing procedures

Cement and both coarse and fine aggregate were mixed for one minute then, the slurry of water, fly ash, and HRWR was added and mixing continued for four minutes to ensure full mixing. The properties of fresh self-compacted concrete were determined by different methods that included the slump, V-funnel and J-ring tests. For examining the effect of test variables on the plastic shrinkage of FSCC, plastic shrinkage tests commenced 15 min after water was first added to the mix. The early-age deformation of fresh concrete was measured by means of an optical apparatus, which is shown schematically in Figures (1 and 2). The details of the apparatus calibration method and procedure for the test were in accordance to ASTM C 827-82[17]. During the tests, the measurements were recorded at regular intervals of time; the final reading was taken 240 min after starting the test. The test samples were left in the moulds to harden overnight and a final measurement was taken 24h after casting. The deformations were converted to shrinkage strain using the expression: $\varepsilon = X/ML$ Where: $\varepsilon =$ plastic shrinkage strain, X = deformation (mm), X = magnification factor and X = height of the specimen (200 mm).

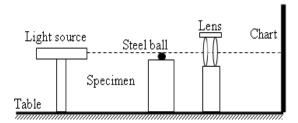




Figure [1] layout of plastic shrinkage apparatus

Figure [2] apparatus for measuring plastic Shrinkage

Testing of FSCC drying shrinkage was carried out according to ASTM C 157 [18]. Three Prismatic specimens of $70\times70\times300$ mm were prepared for each mixture. As the length of the specimen was much larger than the cross-sectional dimensions, then shrinkage was assumed to take place only in the longitudinal direction. The measurement of shrinkage with time can then provide a measure of one-dimensional shrinkage of the tested material. A mechanical gage was used to measure the change in the length of the test specimens at proper time intervals. Figure (3) shows the apparatus of drying shrinkage measurement.



Figure [3] apparatus for measuring dry shrinkage

The shrinkage at Time (t) is calculated by the following equation: Drying shrinkage = Δ L/ Lo; where: Δ L is the measured change in the length and Lo is the original length measured at the start of measurements. After 24 hours of casting, the specimens were removed from the molds and submerged in water at 20°C until testing. A 2000 KN capacity compressive strength testing machine was used to determine of the compressive strength and splitting tensile strength and modules of elasticity. Mixes features are reported in Table (1). In this table, mixture code gives information on the component of the mixes in the concrete. Test specimens were designated by letter C1 or C2 for type of cement used (C1: for cement CEMI 42.5 N) (C2: for cement CEMII/B-L 32.5 N) followed by (H): hooked fibers, (CR) for cramped fibers and (P)

polypropylene fibers. The basic requirements of flowability of FSCC are specified by local technical specification for SCC [19].

Table (1): Mix proportions by weights (Kg/m³)

| Type of cement | Mix code | Vf %* | Cement | Sand | Dolomit e | F.A | HRWR | W |
|--|-------------|-------|--------|------|--------------|-----|------|-----|
| ut ') | CI | 0 | | 996 | 871 | 40 | 6 | 160 |
| | C1H1 | 0.75 | 400 | 940 | 770 | | | |
| | C1H2 | 0.5 | | 924 | 758 | | | |
| Portland cement (CEM I 42.5 N) | C1H3 | 0.2 | | 973 | 798 | | | |
| l ce 42. | C1CR1 | 0.75 | | 940 | 770 | | | |
| and 11 | C1CR2 | 0.5 | 400 | 924 | 758 | | | |
| rtle | C1CR3 | 0.2 | | 973 | 798 | | | |
| Po (C | C1P1 | 0.2 | | 993 | 815 | | | |
| | C1P2 | 0.1 | | 995 | 816 | | | |
| | C1P3 | 0.05 | | 995 | 815 | | | |
| ent 5 N). | C2 | 0 | 400 | 996 | 871 | 40 | 6 | 160 |
| | C2H1 | 0.75 | | 940 | 770 | | | |
| | C2H2 | 0.5 | | 924 | 758 | | | |
| eme 32.5 | C2H3 | 0.2 | | 973 | 798 | | | |
| e co | C2CR1 | 0.75 | | 940 | 770 | | | |
| ton | C2CR2 | 0.5 | | 924 | 758 | | | |
| limestone cement (CEM II/B-L 32.5 N) | C2CR3 | 0.2 | | 973 | 798 | | | |
| | C2P1 | 0.2 | | 993 | 815 | | | |
| | C2P2 | 0.1 | | 995 | 816 | | | |
| | C2P3 | 0.05 | | 995 | 815 | | | |
| C1: CEMI 42.5 N C2: CEMII/B-L 32.5 N H: hooked steel fibers CR: cramped steel fibers | | | | | | | | |

C1: CEMI 42.5 N C2: CEMII/B-L 32.5 N H: hooked steel fibers CR: cramped steel fibers P: polypropylene fibers (*) Fiber volume fraction F.A.: Fly ash

Table (2): Properties of fresh concrete.

| | Mix | Vf %* | result of fresh properties | | | | | | | | |
|--|-------|-------|----------------------------|-----------|----------|------------|----------------------|----------|----------|--|--|
| Type of cement | | | Si | lump test | 1 | J- | Ring | V-Funnel | | | |
| | code | | D_{ave} . | T | | $D_{avr.}$ | H_{in} - H_{out} | T. | velocity | | |
| | | | (mm) | (sec) | T_{50} | (mm) | (cm) | (sec) | (mm/sec) | | |
| ent N) | C1 | 0 | 780 | 6.35 | 3 | 730 | 0.4 | 6.5 | 10 | | |
| | C1H1 | 0.75 | 680 | 7.50 | 3.5 | 650 | 0.7 | 9.2 | 7.065 | | |
| | C1H2 | 0.5 | 730 | 7.25 | 3.25 | 680 | 0.6 | 8 | 8.125 | | |
| me 5 I | C1H3 | 0.2 | 750 | 7.08 | 3.15 | 700 | 0.5 | 7.3 | 8.904 | | |
| l ce 42. | C1CR1 | 0.75 | 650 | 7.45 | 4 | 650 | 0.8 | 10 | 6.5 | | |
| anc A I | C1CR2 | 0.5 | 750 | 7.30 | 3.5 | 690 | 0.6 | 8.5 | 7.647 | | |
| Portland cement (CEM I 42.5 N) | C1CR3 | 0.2 | 770 | 6.55 | 3.45 | 710 | 0.5 | 7.2 | 9.027 | | |
| | C1P1 | 0.2 | 700 | 7.45 | 3.2 | 690 | 0.8 | 9.1 | 7.142 | | |
| | C1P2 | 0.1 | 730 | 7.1 | 3.05 | 700 | 0.6 | 8.3 | 7.831 | | |
| | C1P3 | 0.05 | 750 | 6.55 | 2.50 | 730 | 0.5 | 7.4 | 8.78 | | |
| limestone cement (CEM II/B-L 32.5 N). | C2 | 0 | 750 | 6.25 | 2.5 | 750 | 0.5 | 6.5 | 10 | | |
| | C2H1 | 0.75 | 650 | 8.37 | 3.25 | 650 | 0.8 | 10.3 | 6.310 | | |
| | C2H2 | 0.5 | 700 | 7.40 | 3.11 | 700 | 0.7 | 10 | 6.5 | | |
| | C2H3 | 0.2 | 730 | 6.35 | 2.35 | 720 | 0.6 | 8.3 | 7.831 | | |
| | C2CR1 | 0.75 | 660 | 8.45 | 3.2 | 660 | 0.8 | 11 | 5.909 | | |
| | C2CR2 | 0.5 | 690 | 8.2 | 3.05 | 690 | 0.75 | 9.5 | 6.842 | | |
| | C2CR3 | 0.2 | 720 | 6.5 | 2.5 | 710 | 0.6 | 7.5 | 8.67 | | |
| | C2P1 | 0.2 | 690 | 7.5 | 2.50 | 670 | 0.75 | 10.4 | 6.25 | | |
| | C2P2 | 0.1 | 720 | 6.5 | 2.45 | 690 | 0.6 | 8.4 | 7.73 | | |
| | C2P3 | 0.05 | 750 | 6.25 | 2.35 | 720 | 0.5 | 6.25 | 10.4 | | |

C1: CEMI 42.5 N C2: CEMII/B-L 32.5 N H: hooked steel fibers CR: cramped steel fibers P: polypropylene fibers (*) Fiber volume fraction

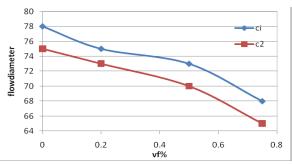
3. RESULTS AND DISCUSSIONS

3.1 Fresh Concrete

Table (2) summarizes the results of testing the properties of fresh SCC mixes. The slump flow ranged from 650 to 780 mm for all mixes. The effect of fiber inclusion on the flowability of SCC was noticed in decreasing the final diameter compared with that of the control mix. The T₅₀ value ranged from 2.5 to 3 seconds for the mixes without fibers and from 2.5 to 4 seconds for those with fibers. The results show that, the fibers have noticeable effect in restricting the flow of FSCC concrete. The original application of the ring test was in conjunction with the slump flow. However, this combination provides a much more powerful tool for the assessment of the fresh properties of fiber self-compacting concrete. For the concrete mixes containing fibers, the difference between the height of the concrete inside and outside the j- Ring was 0.8 cm. While the difference was only 0.45 cm for those without fibers. Both types of fibers, steel and polypropylene, seem to have a regular influence on the blocking criteria of SCC. The basic requirements of flowability were specified by technical specification for SCC [20].

3.1.1 Effect of the cement type on the properties of fresh FSCC

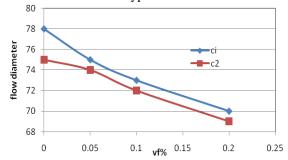
Figures (4 to 9) show the effect of the cement type on the flow diameter of the different mixes. It is noticed that the mixes cast with ordinary Portland cement are more flowable than those with limestone cement by 4% in term of the flow diameter. The effects of percentage of fiber volume fraction are illustrated in Figures (4 to 9). As shown in these figures, the flow diameter decreases as the percentage of volume fraction increased. For example, the mixes cast with ordinary Portland cement and hooked steel fiber had a flow diameter that ranged from 680 to 750 mm. The percentage of reduction ranged from 4% to 14%. The percentage of reduction for the mixes with polypropylene fibers and the ordinary Portland cement ranged from 4% to 10%. The percentage of reduction for the mixes with cramped steel fibers and the ordinary Portland cement ranged from 4% to 17%.



80 78 76 77 70 68 66 64 0 0.2 0.4 0.6 0.8

Figure (4) relationship between volume fraction of hooked end steel fiber and the flow diameter using different types of cement.

Figure (5) relationship between volume fraction of cramped steel fiber and flow diameter using different types of cement.



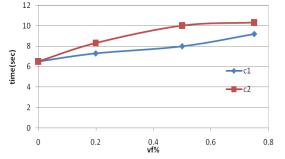
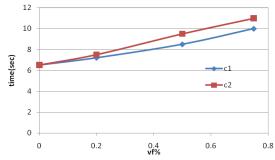


Figure (6) relationship between the volume fraction of polypropylene fiber and the flow diameter using different types of cement.

Figure (7) effect of type of cement of mixes with different ratio of Vf% on the time of V-Funnel Test for hooked end steel fiber..



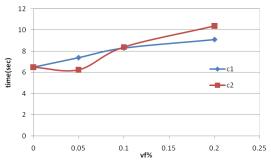


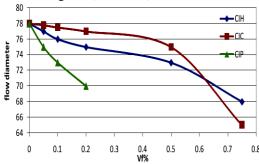
Figure (8) effect of type of cement of mixes with different ratio of VF% on the time of V-Funnel Test for cramped steel fiber.

Figure (9) effect of type of cement of mixes with different ratio of vf% on the time of V-Funnel

Test for polypropylene

3.1.2 Effect of the fibers type on the properties of fresh FSCC

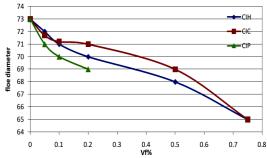
Figures (10 to 13) show the relation between the volume fraction for different types of fibers and the flow diameter. These figures indicate that the flow diameter for the mixes containing cramped steel fibers is larger than the flow diameter of the mixes with hooked steel fibers and those with polypropylene fibers. For examples; at 0.05 V_f the flow diameters were (770, 780 and 750 mm) for the mixes with hooked end steel fibers, cramped steel fibers and polypropylene fibers, respectively. These values were decreased by (1 %, 3.8%, and 10.2%), respectively from the control mix when using ordinary Portland cement as shown in Figure (10). In Figure (11), it can be seen that the flow diameters were (720, 710 and 690 mm) at 0.2 V_f for the mixes with hooked end steel fibers, cramped steel fibers and polypropylene fibers, respectively. These values were decreased by (4 %, 5.3%, and 10.6%), respectively from the control mix when using lime stone cement. At 0.75% V_f the flow diameter decreases by (12% and 16.6%) for hooked end steel fibers and cramped steel fibers, respectively compared the control mix with ordinary Portland cement. At 0.75% V_f the flow diameter decreases by (13%, 12%) for hooked end steel fibers and cramped steel fibers, respectively compared the control mix with ordinary limestone cement. Similar trends were observed from the J-Rring test results as illustrate in Figures (12 and 13) and for V-funnel test results in Figures (14 and 15).



76
74
72
70
68
68
66
64
0 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8

Figure (10) relationship between the volume fraction of fiber and the flow diameter for the mixes using ordinary Portland cement.

Figure (11) relationship between the volume fraction of fiber and the flow diameter using lime stone cement.



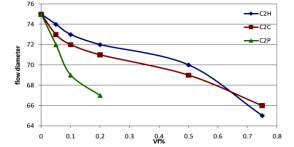
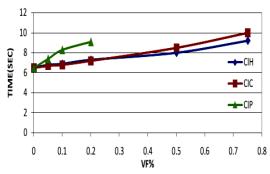


Figure (12) relationship between volume fractions of different types of fibers and the flow diameter of J-Ring test using ordinary Portland cement.

Figure (13) relationship between the volume fraction of fiber and the flow diameter for J-Ring test using lime stone cement



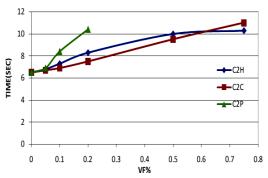


Figure (14) effect of type of fiber with different ratio of VF% on the time of V-Funnel test using ordinary Portland cement.

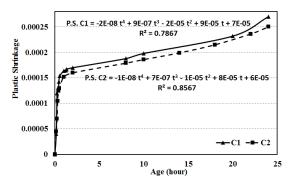
Figure (15) effect of type of fiber with different ratio of VF% on the time of V-Funnel test using lime stone cement.

3.1.3 Effect of cement type on the plastic shrinkage

Figure (16) shows the relationship between the plastic shrinkage and time for the control mixes tested in the laboratory at 58% relative humidity. This figure illustrates that the plastic shrinkage for the C1 mixes is more than the plastic shrinkage for the corresponding C2 mixes. For example, the shrinkage for C1 was 0.00148 after one hour and the shrinkage for the mix with C2 was 0.00075. Thus, the reduction in the plastic shrinkage for the C2 mix compared with that of C1 mix was 49 %. After 24 hours, the reduction in the plastic shrinkage for the mix C2 is less than that mix of C1 by 7%. This result is supported by a previous study conducted by Timothy Barrett [21]. The reasons for the difference in the plastic shrinkage is attributed to the inter-ground materials in limestone cement are slightly finer that the ordinary cement. Also, limestone cement has fewer particles above 30 microns in size. The production of lime stone cement uses a grinding and separation process that eliminates the largest cement particles while creating very finely ground limestone particles. The removal of the large cement particles allows lime stone cement mixtures to have pore size distributions that are similar to ordinary Portland cement, showing that pore size distribution has more of an effect on shrinkage than fineness [21-22].

3.1.4 Effect of fiber types on the plastic shrinkage

Figures (17 to 19) show the relationship between the plastic shrinkage and elapsed time for the different mixes containing different types of fibers with the same percentage of volume fraction compared to the control mixes without fibers. Figure (19) shows that the plastic shrinkage of the mixes with polypropylene fibers was more than the plastic shrinkage for those with hooked end and cramped circular section steel fiber at 0.2% V_f. It was noticed that, the plastic shrinkage wasn't improved at this percentage of all types of fiber compared to the control mix with ordinary Portland cement. Generally, the plastic shrinkage for the mixes with these percentage polyproblen fibers was larger than that of the control mix. For example, the plastic shrinkage at one hour for the mix with polypropylene fiber was equal to 0.000185, while the shrinkage for the mix with hooked end and crimped circular section steel fiber was 0. 0.00011, 0.00014; respectively. The maximum plastic shrinkage was 0.000281, 0.000248, and 0.000252 for the mixes with polypropylene, hooked end and crimped steel fibers; respectively. The maximum plastic shrinkage for the mixes with polypropylene fiber increased by 3.7%, while the maximum plastic shrinkage for the mixes with hooked end steel fiber and cramped steel fiber was decreased by 8.15% and 6.7%; respectively. The plastic shrinkage of the mix with crimped steel fibers and hooked end steel fibers was improving compared to the control mix, while it didn't improve due to the polypropylene fibers. For example, at 0.2 % Vf, the plastic shrinkage at one hour for the mix with polypropylene fiber, was 0.00016; while the shrinkage of that with hooked end and crimped circular section steel fibers was 0.000054 and 0.000135, respectively. The maximum plastic shrinkage for the mixes with cramped steel and hooked steel fiber decreased by 0% and 8%, respectively while the maximum plastic shrinkage for the mixes with polypropylene fibers was increased by 10% compared to the control mix with lime stone cement.



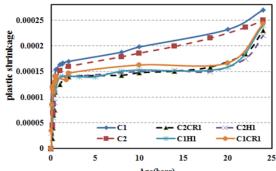
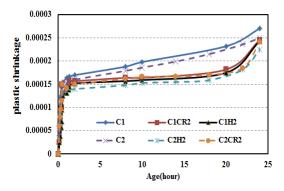


Figure (16) relationship between plastic shrinkage and ages (hours) for control mixes.

Figure (17) relationship between plastic shrinkage and ages (hour) for mixes with 0.75 % volume fraction for different types of steel



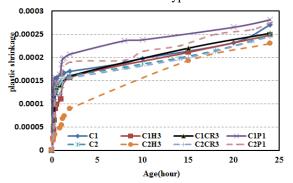


Figure (18) relationship between plastic shrinkage and ages (hour) for mixes with 0.5 % volume fraction for different types of steel fiber

Figure (19) relationship between plastic shrinkage and ages (hour) for mixes with 0.2 % volume fraction for different types of fiber.

3.1.5 Effect of fiber volume fraction on plastic shrinkage

Figure (20) shows the relationship between the max plastic shrinkage for the different mixes containing different types and values of Vf using ordinary Portland cement and limestone cement. It can be seen that as the volume fraction increase the plastic shrinkage decreased. The plastic shrinkage for the mix containing hooked steel fibers at 0.75 Vf is less than the plastic shrinkage for mix with 0.5 Vf and 0.2 Vf. The maximum plastic shrinkage for the mixes with 0.75, 0.5 and 0.2 Vf decreased by 10%, 9.3% and 8% of the control mix, respectively. The same results were noticed for the cramped steel fibers. The maximum plastic shrinkage for the mixes with 0.75, 0.5 and 0.2 Vf decreased by 10%, 9.3% and 6.7% of the control mix, respectively. The plastic shrinkage for the mixes with polypropylene is more than the plastic shrinkage for control mix. On the other hand the plastic shrinkage decreased as the volume fraction increase. The maximum plastic shrinkage for the mixes with 0.2, 0.1 and 0.05 Vf increased by 4%, 18.5% and 33.3% of the control mix, respectively. The relationship between the maximum plastic shrinkage and Vf % for different mixes using limestone cement was showed in the same figure. It can be seen that the plastic shrinkage decreases as the fiber volume fraction increased. The plastic shrinkage for the mixes with polypropylene more than the plastic shrinkage for control mix. It is noticed that, the plastic shrinkage didn't improved by using the polypropylene fiber compared to the control mix. The maximum plastic shrinkage for the mixes with 0.05Vf, 0.1Vf and 0.2Vf increased by 20%, 12% and 10%, respectively compared with the control mix. Empirical colorations were formulated for maximum plastic shrinkage and the volume fraction percent for the different mixes as shown in figure (20). The relation between plastic shrinkage and time was forth order polynomial form with R-square value =1.

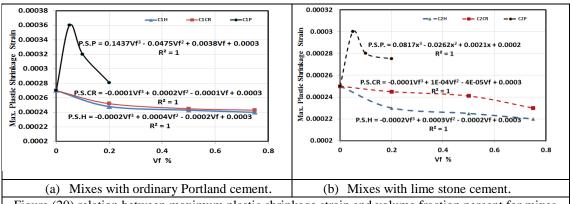


Figure (20) relation between maximum plastic shrinkage strain and volume fraction percent for mixes with different types of fibers.

3.2 Properties of hardened Fiber self-compacted concrete

From Tables 3 and 4: it was found that fiber addition has a slight effect on the properties of hardened FSCC.

Table [3] Strength results of the mixes with ordinary Portland cement

| Mix code | CI | C1H1 | C1H2 | С1Н3 | C1CR1 | C1CR2 | C1CR3 | C1P1 | C1P2 | C1P3 |
|-----------------------------------|------|------|------|------|-------|-------|-------|------|------|------|
| Compressive strength (MPa) | 52.0 | 59.0 | 52.0 | 54.0 | 52.0 | 56.0 | 52.0 | 56.0 | 59.0 | 56.0 |
| Indirect tensile strength (MPa) | 8.0 | 8.0 | 12.0 | 9.0 | 7.0 | 9.0 | 8.0 | 7.0 | 9.0 | 7.0 |
| Modulus of elasticity (MPa) *10^4 | 2.75 | 3.12 | 2.88 | 2.84 | 2.76 | 2.91 | 2.87 | 2.72 | 3.2 | 2.95 |

Table [4] Strength results of the mixes with limestone cement

| Mix code | C 2 | C2H1 | C2H2 | С2Н3 | C2CR1 | C2CR2 | C2CR3 | C2P1 | C2P2 | C2P3 |
|-----------------------------------|------|------|------|------|-------|-------|-------|------|------|------|
| Compressive strength (MPa) | | 48.0 | 49.0 | 48.0 | 45.0 | 44.5 | 44.0 | 49.0 | 49.0 | 47.0 |
| Indirect tensile strength (MPa) | 8.0 | 8.0 | 11.0 | 7.0 | 10.0 | 8.0 | 8.0 | 10.0 | 8.0 | 8.0 |
| Modulus of elasticity (MPa) *10^4 | 2.38 | 2.83 | 3.1 | 2.78 | 2.41 | 2.25 | 2.32 | 3.07 | 3.08 | 2.69 |

3.3 Drying Shrinkage:

3.3.1 Effect of cement type:

Figure (21) illustrates the relationship between shrinkage strain and elapsed time (age, days) for the control mixes at different weather conditions. Generally, the shrinkage strain for the mix with limestone cement is less than the shrinkage for ordinary Portland cement. For example, the shrinkage for the mix with limestone cement was 0.064 at 10 days, while the shrinkage for mix with ordinary Portland cement was 0.1226. On the other hands, the corresponding shrinkage measurements were 0.0349 and 0.043 at 100 days. The maximum shrinkage strain was measured at 210 days and the shrinkage measurements were 0.0495 and 0.0387 for OPC and L.C, respectively. However, these measurements were reducing to 0.0447 and 0.03339, respectively by the end of the experimental at 320 days. Empirical colorations were formulated for dry shrinkage and the time for the mixes with different types of cement as shown in figure (21). The relation between plastic shrinkage and time was forth order polynomial form with R-square value varied between 0.96 and 0.92.

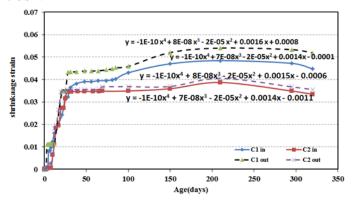
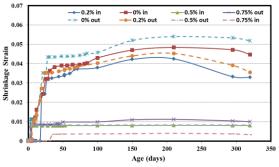


Figure (21) Relationship between shrinkage strain and ages for control mixes in air laboratory and atmosphere

3.3.2 Effect of fiber volume fraction

Figures (22 to 24) show the relationship between the shrinkage strains and elapsed time for different mixes containing different fiber percentage (Vf %) using ordinary Portland cement in the laboratory and open atmosphere. Using fibers decreased the drying shrinkage of the mixes compared to the control mix. As the volume fraction increase the dry shrinkage decreased. These results were supported by a previous study conducted by Eren Ö.; and Marar K. [23] and Aly T. et. al. [24] these results were noticed in the laboratory and open atmosphere. The effect of different volume fraction of hooked end steel fiber on the drying shrinkage compared to the control mix without fiber in the laboratory and open atmosphere was explained in Figure (22). The shrinkage strain was 0.00072, 0.0789 and 0.0012 at 10 days for mixes with 0.75, 0.5 and 0.2 Vf%, respectively. On the other hands, the corresponding shrinkage measurements were 0.0371, 0.0801 and 0.379 for mixes with 0.75, 0.5 and 0.2 Vf% at 100 days. The maximum shrinkage strain was measured at 210 days and the shrinkage measurements were 0.0399, 0.0815 and 0.462 for the mixes with 0.75, 0.5 and 0.2 Vf %, respectively. However, these measurements were reduced to 0.00327, 0.008 and 0.033, respectively by the end of the experimental at 320 days. The drying shrinkage for the mixes with 0.75 %, 0.5 % and 0.2 % Vf reduced by 26.2%, 82.1% and 92.6%, respectively compared to the control mix without fibers. These results were in the laboratory. The shrinkage strain was 0.00847, 0.00814 and 0.01344 at 10 days for mixes with 0.75, 0.5 and 0.2 Vf% respectively. On the other hands, the corresponding shrinkage measurements were 0.0099, 0.00827 and 0.041 for mixes with 0.75, 0.5 and 0.2 Vf% at 100 days. The maximum shrinkage strain was measured at 210 days and the shrinkage measurements were 0.0112, 0.00832 and 0.04843 for the mixes with 0.75, 0.5 and 0.2 Vf %, respectively. However, these measurements were reduced to after that the shrinkage strain was reduced to 0.01, 0.00826 and 0.0355, respectively by the end of the experimental at 320 days. The drying shrinkage for the mixes with 0.75 %, 0.5 % and 0.2 % Vf reduced by 31.5%, 82.1% and 80.7%, respectively compared to the control mix without fibers. These results were in open atmosphere. The same results were noticed and recorded for the cramped steel and polypropylene fibers as in Figures (23 and 24).



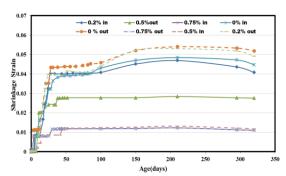


Figure (22) Relation between shrinkage strain and age for mixes with different fiber percentages for hooked end steel fiber using ordinary Portland

Figure (23) Relation between shrinkage strain and age for mixes with different fiber percentages for cramped steel fiber using ordinary Portland cement.

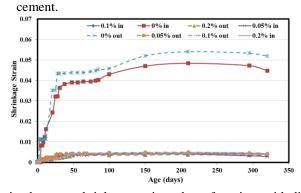
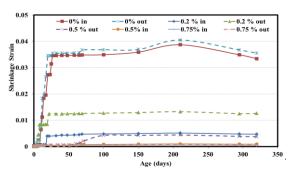


Figure (24) Relation between shrinkage strain and age for mixes with different fiber percentages for polypropylene fiber using ordinary Portland cement.

Figures (25 to 27) show the relationship between the shrinkage strains and elapsed time for different mixes containing different fiber percentages (Vf%) using limestone cement in the laboratory and open

atmosphere. The use fibers decreased the drying shrinkage of the mixes compared to the control mix. These results were noticed in the laboratory and open atmosphere. The effect of different volume fraction of hooked steel fiber on the drying shrinkage compared to the control mix without fiber in the laboratory and open atmosphere was explained in Figure (25). This Figure shows that as the volume fraction increase the dry shrinkage decreased. The shrinkage strain was 0.0003, 0.000376 and 0.000536 at 10 days for mixes with 0.75, 0.5 and 0.2 Vf%, respectively. On the other hands, the corresponding shrinkage measurements were 0.00045, 0.0008 and 0.0048 for mixes with 0.75, 0.5 and 0.2 Vf % at 100 days. The maximum shrinkage strain was measured at 210 days and the shrinkage measurements were 0.00051, 0.001 and 0.00511 for the mixes with 0.75, 0.5 and 0.2 Vf %, respectively. However, these measurements were reduced to after that the shrinkage strain was reduced to 0.00042, 0.0009and 0.00468, respectively by the end of the experimental at 320 days. The drying shrinkage for the mix with 0.75%, 0.5% and 0.2% Vf reduced by 99%, 97.9% and 89.5%, respectively compared to the control mix without fibers. These results were in the laboratory. The shrinkage strain was 0.004, 0.0032 and 0.08292 at 10 days for mixes with 0.75, 0.5 and 0.2 Vf%, respectively. On the other hands, the corresponding shrinkage measurements were 0.0059, 0.0423 and 0.127 for mixes with 0.75, 0.5 and 0.2 Vf % at 100 days. The maximum shrinkage strain was measured at 210 days and the shrinkage measurements were 0.0069, 0.04364 and 0.1324 for the mixes with 0.75, 0.5 and 0.2 Vf %, respectively. However, these measurements were reduced to after that the shrinkage strain was reduced to 0.00053, 0.00368 and 0.0126, respectively by the end of the experimental at 320 days. The drying shrinkage for the mix with 0.75%, 0.5% and 0.2% Vf reduced by 98.9%, 92.9% and 75.7%, respectively compared to the control mix without fibers. These results were in open atmosphere. The same results were noticed and recorded for the cramped steel and polypropylene fibers as in Figures (26 and 27).



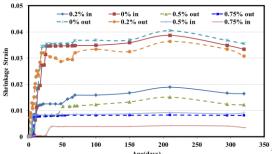


Figure (25) Relation between shrinkage strain and age for mixes with different fiber percentages for hooked steel fiber using limestone cement.

Figure (26) Relation between shrinkage strain and age for mixes with different fiber percentages for cramped steel fiber using limestone cement.

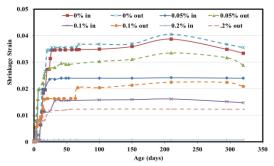


Figure (27) Relation between shrinkage strain and age for mixes with different fiber percentages for polypropylene fiber using limestone cement.

3.3.3 Effect of weather conditions

The effect of weather conditions on the shrinkage strain is shown in Figure (21). The Figure shows that the shrinkage strain for the mixes in the laboratory was less than the shrinkage strain in open atmosphere. For example, the shrinkage strain for the mix with limestone cement in the laboratory was 0.0385 at 200 days. This value was less than the shrinkage strain for the mix in open atmosphere by 6.3 %. The change in the shrinkage strain occurred due to the change in the relative moisture content that changes from 34% to 45%, so the higher the relative moisture content caused, the lower the rate of shrinkage. Also, the lower

temperature gradient caused the lower rate of shrinkage. The same observations were recorded for the mix with ordinary Portland cement. On the other hand, the effect of using fiber was shown in figures (22 to24) for the mixes with ordinary Portland cement and figures (25 to 27) for the mixes with limestone cement. For example the shrinkage strain for the mix with 0.75 Vf% cramped steel fiber with Portland cement in the laboratory was 0.00434 at 200 days as illustrated in figure (22). This value was less than the shrinkage strain for the mix in open atmosphere by 67.4 %. Also, the shrinkage strain for the mix with 0.75 Vf % cramped steel fiber with limestone cement in the laboratory was 0.00398 at 200 days illustrated in figure (25). This value was less than the shrinkage strain for the mix in open atmosphere by 57.4%. The same trends were recorded for the mixes with different values of volume fraction. The change in the shrinkage strain occurred due to the change in the relative moisture content can be eliminated by using the fibers. For example, the maximum shrinkage strain was measured at 210 days and the shrinkage measurements were 0.4951 for the control mix with ordinary Portland cement. However, these measurements were reduced to after that the shrinkage strain was reduced by 9.6 % by the end of the experimental at 320 days. On the other hand, the maximum shrinkage strain was measured at 210 days and the shrinkage measurements were 0.00399 for the mixes with 0.75 Vf% hooked steel fibers. However, these measurements were reduced to 0.00487 after that the shrinkage strain was reduced by 18% by the end of the experimental at 320 days. Empirical colorations were formulated for dry shrinkage and the time for the mixes with different types of cement as at different weather conditions as shown in figure (21). The relation between plastic shrinkage and time was forth order polynomial form with R-square value varied between 0.96 and 0.92.

3.3.4 Influence of the fiber type

Figures (28 to 30) show the relationship between the shrinkage strains and elapsed time for different types of fibers at the same value of Vf% using ordinary Portland cement in the laboratory and open atmosphere. Using polypropylene fibers decreased the drying shrinkage of the mixes more than steel fibers. Also, Using hooked steel fibers decreased the drying shrinkage compared to the cramped steel fibers. The results were noticed for the laboratory and open atmosphere conditions. For example; Figure (28) shows the relation between the drying shrinkage and ages at 0.2 % volume fraction for different types of fibers. The drying shrinkage for the mixes with hooked steel fiber was less than the drying shrinkage for mixes with cramped steel fibers. Also, the drying shrinkage for steel fibers mixes was less than the drying shrinkage of the control. The maximum shrinkage strain was measured at 210 days and the shrinkage measurements were 0.04843 and 0.056 for the mixes with hooked steel fiber and cramped steel fibers, respectively. 13.5 percent decreasing in the max drying shrinkage strain for the mix with hooked steel fibers to cramped steel fibers mixes. However, these measurements were reduced to 0.0355 and 0.0491, respectively by the end of the experimental at 320 days. The same results were noticed and recorded in the open atmosphere. In Figures (28) the drying shrinkage for the mixes with polypropylene fibers was less than the drying shrinkage for the mixes with steel fibers. The maximum shrinkage strain was measured at 210 days and the shrinkage measurements were 0.0372. However, the measurements were reduced to 0.0348 by the end of the experimental at 320 days. 23.2 percent decreasing in the maximum drying shrinkage for the mixes with polypropylene fibers compared to the steel fibers mixes at 210 days. Also, 29.1 percent increasing in the shrinkage by the end of the experimental at 320 days. The same observations were recorded in the open atmosphere.

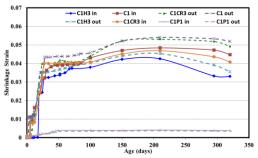


Figure (28) relation between shrinkage strain and age at 0.2 % volume fraction for different types of fibers using ordinary Portland cement.

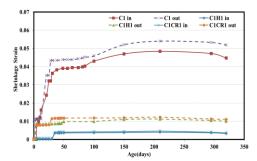


Figure (29) relation between shrinkage strain and age at 0.75 % volume fraction for different types of steel fibers using ordinary Portland cement.

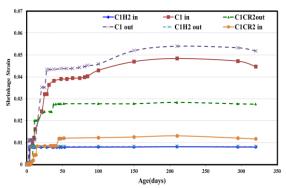
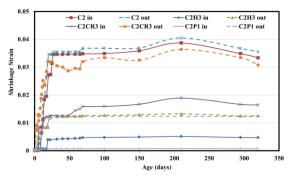


Figure (30) relation between shrinkage strain and ages at 0.5 % volume fraction for different types of steel fibers using ordinary Portland cement.

Figures (31 to 32) show the relationship between the shrinkage strains and elapsed time for different types of fibers at the same value of Vf % using limestone cement in the laboratory and open atmosphere. These figures show that using polypropylene fibers decreased the drying shrinkage of the mixes more than steel fibers. Also, using hooked steel fibers decrease the drying shrinkage more than cramped steel fibers. All types of fibers improved the drying shrinkage compared to the control mix. These results were noticed in the laboratory and open atmosphere conditions. For example; Figure (32) shows the relation between the drying shrinkage and age at 0.75% volume fraction for different types of steel fibers. The drying shrinkage for the mix with hooked steel fiber was less than the drying shrinkage for mix with cramped steel fibers. Also, the drying shrinkage for steel fibers mixes was less than the drying shrinkage of the control. The maximum shrinkage was measured at 210 days and the shrinkage measurements were 0.0364 and 0.01342 for the mixes with cramped steel fibers and hooked steel fibers, respectively. However, these measurements were reduced to 0.0308 and 0.0126, respectively by the end of the experimental at 320 days. The same results were noticed in the open atmosphere. In Figure (31) the drying shrinkage for the mixes with polypropylene fibers was less than the drying shrinkage for the mixes with steel fibers. The maximum shrinkage strain was measured at 210 days and the shrinkage measurement was 0.01236. However this measurement was reduced to 0.01227 at the end of the experimental at 320 days. 66 percent was decreasing in the maximum drying shrinkage for the mix with polypropylene fibers compared to the steel fibers mix. Also, 60.2 percent decreasing in the shrinkage strain at the end of the experimental at 320 days. The same observations were recorded in open atmosphere.



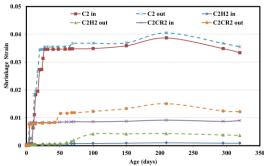


Figure (31) relation between shrinkage strain and age at 0.2 % volume fraction for different types of fibers using limestone cement.

Figure (32) relation between shrinkage strain and ages at 0.5 % volume fraction for different types of steel fibers using limestone cement.

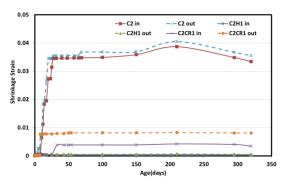


Figure (33) relation between shrinkage strain and age at 0.75 % volume fraction for different types of steel fibers using limestone cement.

The Empirical colorations for drying shrinkage and the time for the mixes with different types of cement at different weather conditions were formulated as shown in figure (34) to figure (43). The relation between plastic shrinkage and time was forth order polynomial form with R-square value varied between 0.75 and 0.95.

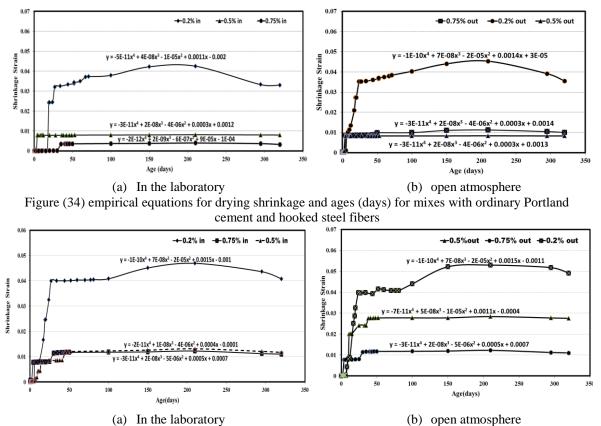


Figure (34) empirical equations for drying shrinkage and ages (days) for mixes with ordinary Portland cement and cramped steel fibers

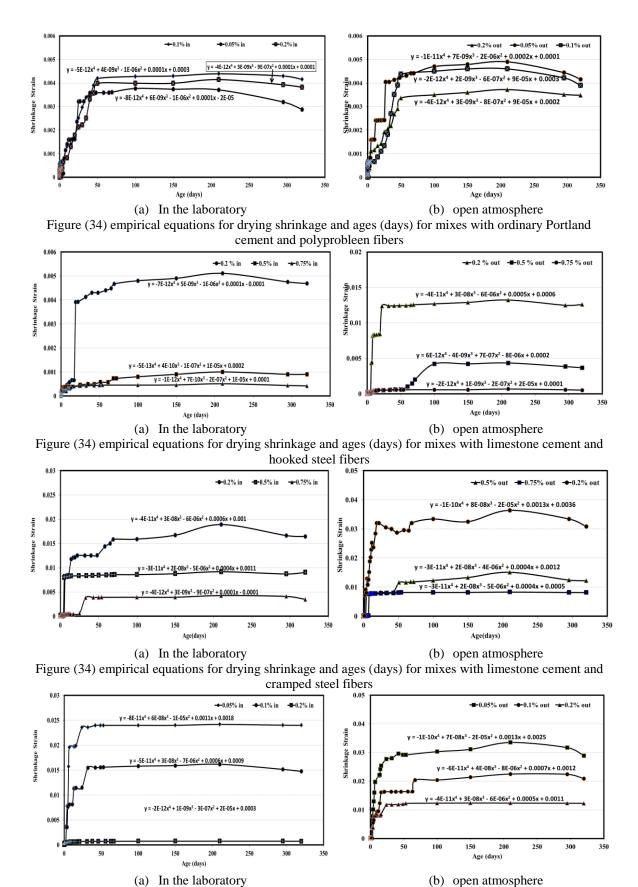


Figure (34) empirical equations for drying shrinkage and ages (days) for mixes with limestone cement and polypropylene fibers

4. CONCLUSIONS

The following conclusions could be drawn from the results of the research carried out to determine strength and shrinkage of self-compacting fiber reinforced concrete:

- 1- The mixes cast with ordinary Portland cement yielded higher flowability compared to similar mixes cast with limestone cement by 4%.
- 2- The flowability of the mixes was reduced due to the use of fibers. In case of Portland cement: the reduction in the flow diameter ranged from (3.8 % to 13%) for hooked steel fiber; (1.3% to 17%) for cramped steel fibers and (3.8% to 10.3%). for polypropylene fibers. In case of limestone cement; the reduction in the flow diameter ranged from (2.7 % to 13.3%) for hooked steel fibers, (4% to 12%) cramped steel fibers and (0% to 8%) for polypropylene fibers.
- 3- The plastic shrinkage for the mix with ordinary Portland cement was higher than that for similar mixes with limestone cement. The maximum plastic shrinkage was lower by 7.4% for the mixes with limestone cement compared to the mixes with Portland cement.
- 4-The plastic shrinkage for the mixes with polypropylene was more than that for both control mixes with ordinary Portland cement and limestone cement. The maximum plastic shrinkage for the mixes with polypropylene fiber increased by 33% and 20% compared with the control mix with ordinary Portland cement and limestone cement and without fibers, respectively.
- 5- The maximum plastic shrinkage for the mixes with hooked steel fiber and cramped steel fiber decreased by 8% and 6.7%, respectively compared with the control mix with ordinary Portland cement.
- 6- The maximum plastic shrinkage for the mixes with hooked steel and cramped steel fiber decreased by 8% and 2%, respectively compared the control mix with limestone cement.
- 7- The drying shrinkage increased up to 210 days after that the drying shrinkage decreased for all mixes. The average value of decreasing was 12% compared to maximum value of drying shrinkage for the mixes.
- 8- The maximum drying shrinkage for the mix with limestone cement decreased by 20% and 25% compared with the mix with ordinary Portland cement in the laboratory and open atmosphere, respectively.
- 9- The maximum drying shrinkage in the laboratory was less than that in the open atmosphere by 11.6% and 5.0% for the mixes with ordinary Portland and limestone cement, respectively.
- 10- The use of fibers reduced the drying shrinkage compared to the control mix. Also the drying shrinkage decreased as the volume fraction increases. These results were noticed in the laboratory and open atmosphere.
- 11-Using polypropylene fibers decreased the drying shrinkage of the mixes more than using steel fibers for two types of cement. The average drying shrinkage for the mix with polypropylene fibers decreased by 91.6 % and 53.4 % compared with the steel fibers mix with ordinary Portland cement and lime stone cement, respectively.
- 12- Using hooked steel fibers decreased the drying shrinkage more than cramped steel fibers. The average drying shrinkage for the mixes with hooked steel fibers decreased by 37.6 % and 79% compared with the mix with cramped steel fibers for both ordinary Portland cement and limestone cement, respectively.
- 13- The change in the shrinkage strain occurred due to the change in the relative moisture content can be eliminated by using the fibers.
- 14- The fiber addition has a slight effect on the properties of hardened fiber self-compacted concrete.
- 15- An empirical equations for plastic and drying shrinkage with time were formulated for the mixes with different types of fibers at different weather conditions.
- 16- Extensive applications could be achieved especially for liquid constrainers and prestressed elements duo to the plastic and dry shrinkage, which was reached by adding different types of fibers to the self-compacted concrete mixes.

REFERENCES

- [1] A Yahai, M.tanimura, A.Shimabukuro and Y Shimayama, "Effects of Rheological Parameters on Self Compact Ability of Concrete Containing Various Mineral Admixtures". Ist International RILEM symposium, Stockholm, Swedeh 13-14 september 1999.
- [2] Okamura H. and Ouchi M.," Self-Compacting Concrete. Development present use and future", Proceeding of the 1st International Symposium on Self-Compacting Concrete, pp. 3-14, Stockholm, 1999.
- [3] American Concrete Institute (ACI 209.1R-05), "Report on Factors Affecting Shinkage and Creep of Hardened Concrete." American Concrete Institute, Detroit, Michigan, 2005.

- [4] Esping O., "Rheology of cementitious material: effects of geometrical properties of filler and fine aggregate", Chalmers University of Technology, Goteborg, 2004.
- [5] Ferraris, C.F. Karthik H.O. and Russell H.,"The Influence of Mineral Admixtures on the Rheology of Cement Paste and Concrete", Cement and Concrete Research, Vol.31,pp.245-255,2001.
- **[6] Gallias J.L.**," The Effect of Fine Mineral Admixtures on Water Requirement of Cement Pastes", Cement and Concrete Research, 2000, 30,pp.1543-1549.
- [7] Powers T. C., "The Properties of fresh concrete", New York, 1968.
- [8] Neville, A.M., Dilger, W.H., and Brooks J.J., "Creep of plain and Structural Concrete", Construction press, 1983, 361 p.
- [9]Kovler K., "Why Sealed Concrete Swells", ACI Materials Journal, 1996, 93 (4), pp.334-340.
- [10] B. E. Bucher, "Shrinkage and shrinkage cracking behavior of cement systems containing ground limestone, fly ash, and lightweight synthetic particles," Civil Engineering M.S.C.E., Civil Engineering, United States -- Indiana, 2009.
- [11] Bucher B., Radlinska and A., Weiss J., "Preliminary Comments on Shrinkage and Shrinkage Cracking Behavior of Cement Systems that Contain Limestone," Proceedings from NRMCA Concrete Technology Forum: Focus on Sustainable Development, May 2008.
- [12] **Kar S. and Sanjay S. S. (2016)** "Effect of Admixtures on Shrinkage Properties in Self Compacting Concrete" International Journal of Research in Engineering and Technology. 2016, 5 (2), pp.292-296
- [13] **Ghezal A. and Assaf G.** "Time-Dependent Behavior of Self-Consolidating Concrete Loaded at Early Age: Influence of Chemical Admixtures." Journal of Materials in Civil Engineering, January 2016, 28 (1), 2016.
- [14] Egyptian Standard Specifications 4765-1/2009, "Composition, Specification and Conformity Criteria of Common Cements", Egyptian Organization for Standardization and Quality Control, 2009,48 pp.
- [15] ASTM C618: Specification for fly ash and raw calcined natural pozzolan for use as a mineral admixture in Portland cement concrete, Annual Book for ASTM Stand, 2002, 4, 4p.
- [16] ASTM C494/C 494M, "Standard Specification for Chemical Admixtures for Concrete", Annual Book of ASTM Standards 2001, 04, 02, p.9.
- [17] ASTM C827/C827M-10, "Standard Test Method for Change in Height at Early Ages of Cylindrical Specimens of Cementitious Mixtures" 2010.
- [18] ASTM C157/C157M-08(2014)E1, Standard Test Method for Length Change of Hardened Hydraulic-Cement Mortar and Concrete, 2014.
- [19] Technical specifications for self-compacted concrete, national building research center, Cairo, Egypt, 2007.
- [20] Timothy Barrett, Hongfang Sun, Chiara Villani and Laurent Barcelo., "Performance of More Sustainable Cements that Include Interground Limestone Additions of up to 15%," Joint Transportation Research Program, Indiana Department of Transportation and Purdue University, West Lafayette, Indiana, 2013.
- [21] Barrett T., Sun H., Villani C., Barcelo L. and Weiss J. "Portland Limestone Cement: Early Age Shrinkage Behavior". Concrete International 2014; 36 (2).
- [22] Hawkins P., Tennis P. and Detwiler R. "The Use of Limestone in Portland Cement: A State-of-the-Art Review" Portland Cement Association 2003 ISBN: 0-89312-229-7 EB227, Portland Cement Association, Skokie, Illinois, USA, 2003, 44 pages.
- [23] Eren Ö. and Marar K. "Effect of steel fibers on plastic shrinkage cracking of normal and high strength concretes" Mat. Res. 2010, 13 (2).

http://dx.doi.org/10.1590/S1516-14392010000200004 (accessed at 3/2016)

[24] Aly T., Sanjayan J. G. and Collins E F. "Effect of polypropylene fibers on shrinkage and cracking of concretes" Materials and Structures. 2008, 41, pp.1741–1753

https://www.researchgate.net/publication/225159578_ (accessed Apr 22, 2016).